

# Erratum: Long-Range Frustration in a Spin-Glass Model of the Vertex-Cover Problem [Phys. Rev. Lett. 94, 217203 (2005)]

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Some mistakes in the Letter [H. Zhou, Phys. Rev. Lett. 94, 217203 (2005)] are corrected.

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We found several mistakes in the Letter [1], which significantly affect the quantitative theoretical results.

The expression (5) for the long-range frustration order parameter  $R$  was wrong. For an unfrozen vertex  $i$  to be type-I unfrozen in graph  $G$ , one of its nearest neighbors (say  $j$ ) must be positively frozen and facing the local environment of type (ii) in  $G'$  (the graph obtained by removing  $i$  and its edges from  $G$ ). The correct formula for  $R$  is

$$R = \frac{cq_+^2}{q_0} \left( 1 - \frac{1}{q_+} e^{-cq_+ - cq_0 R} \right).$$

$R$  as a function of the mean vertex degree  $c$  is shown in the corrected Fig. 1. It is positive for  $c > e = 2.718\dots$  and its maximum is reached at  $c \simeq 14.85$ .

The self-consistent equation (4) for the size distribution  $f(s)$  was wrong. The quantity  $p_1$  of this expression should be replaced by  $p'_1 = p_1/(1-R)$ , which is the conditional probability that a vertex  $i$  faces the environment of type (iii) given that  $i$  is a type-II unfrozen vertex in  $G$ . The function  $f(s)$  satisfies  $\sum_{s=0}^{\infty} f(s) = 1$ .

Equation (6) for the fraction of covered vertices  $X_{\min}$  was also wrong. According to the analysis in [2], the correct formula should be

$$X_{\min} = \frac{1}{c} \int_0^c [1 - q_+(c')] dc',$$

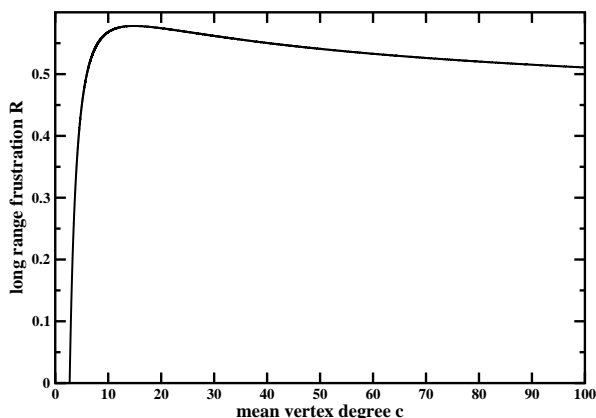


FIG. 1: The long-range frustration order parameter  $R$ .

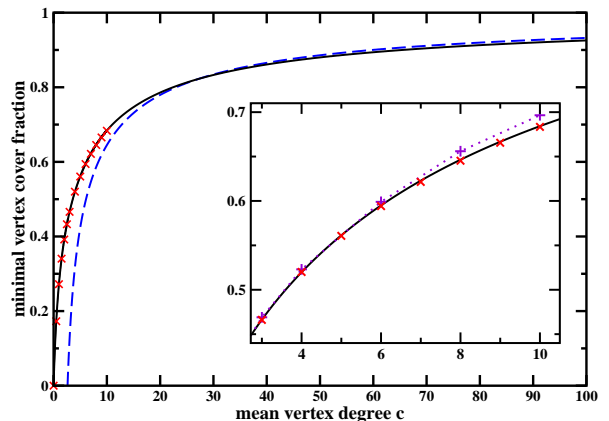


FIG. 2: (color online). The minimal vertex-cover fraction  $X_{\min}$  (solid line) and its comparison with the asymptotic formula of Ref. [3] (dashed line), the numerical results of Ref. [4] ('+' symbols) and Ref. [5] ('x' symbols).

where  $q_+(c)$  is the fraction of positively frozen vertices at mean vertex degree  $c$ .  $X_{\min}$  as a function of  $c$  is shown in the updated Fig. 2. The theoretical prediction is in agreement with simulation results obtained on single large graphs [5], it is slightly lower than the enumeration result obtained on single small graphs [4]. When the mean vertex degree  $c$  is large, the value of  $X_{\min}$  is slightly lower than the asymptotic result of [3].

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